

Geodesy 1 (GED203) Section No: 9

Types of Conditions in Triangulation Networks

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- What is meant by conditions?
- Types of conditions
- Different methods to compute internal conditions
- Examples

➤ **Scale**

The computed length of a side must equal its known length or differ by a value within tolerance.

➤ **Orientation**

The computed azimuth of a side must equal its known azimuth or differ by a value within tolerance.

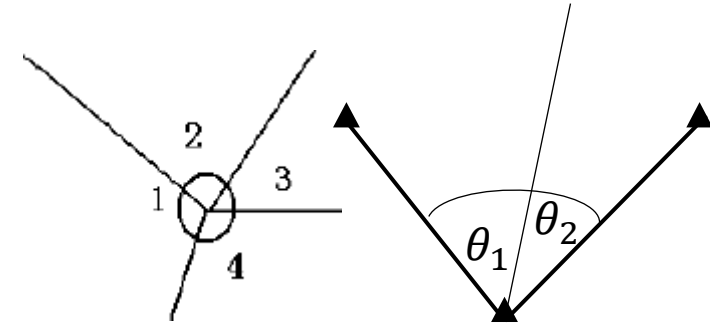
➤ **Position**

The computed coordinates of a point must equal its known coordinates or differ by a value within tolerance.

Internal (Geometric) Conditions

➤ Local condition

The sum of angles taken at certain station should equal a pre-specified value.

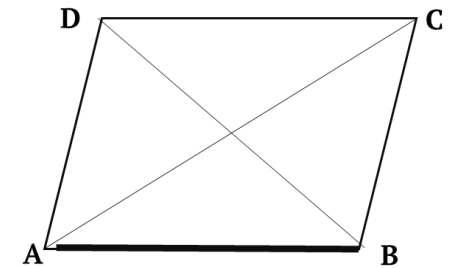


➤ Side condition

The length of a side should equal specific value whatever the route used in calculation.

➤ Angle / Triangle condition

The sum of the internal angles of a polygon should equals $(n - 2) \times 180^\circ + \varepsilon$



How to calculate the number of different types of internal conditions?

(1) By Law

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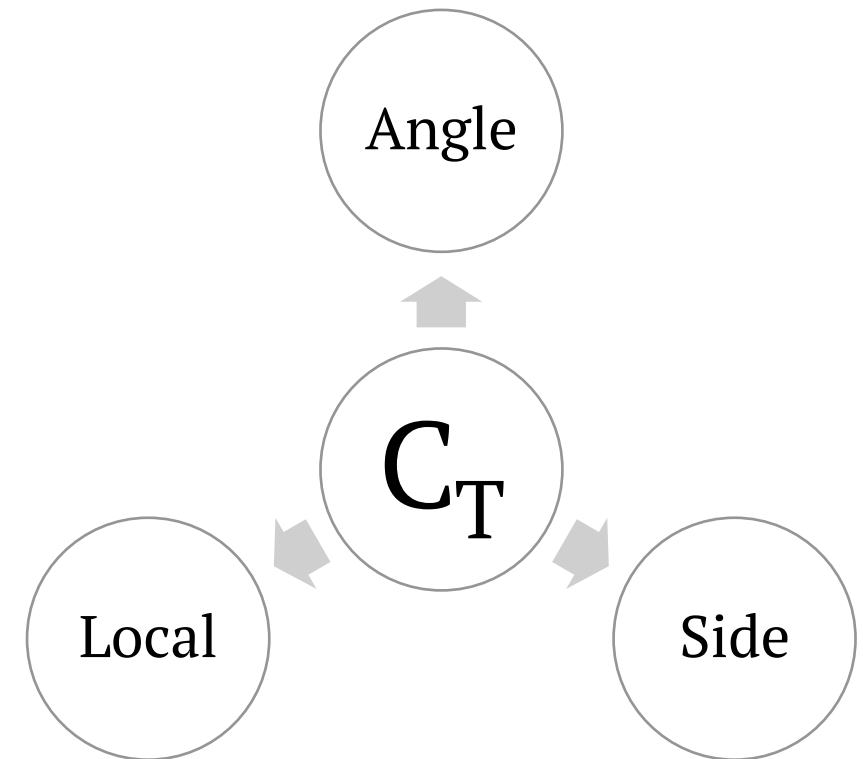
➤ The total number of geometric conditions C_T in a figure is:

$$C_T = O_T - O_{nec.}$$

Where:

O_T Total number of observations

$O_{nec.}$ Number of necessary observations



(1) By Law

(1) Angle Conditions

➤ The total number of geometric conditions C_A in a figure is:

$$C_A = (L - L') - (S - S') + 1$$

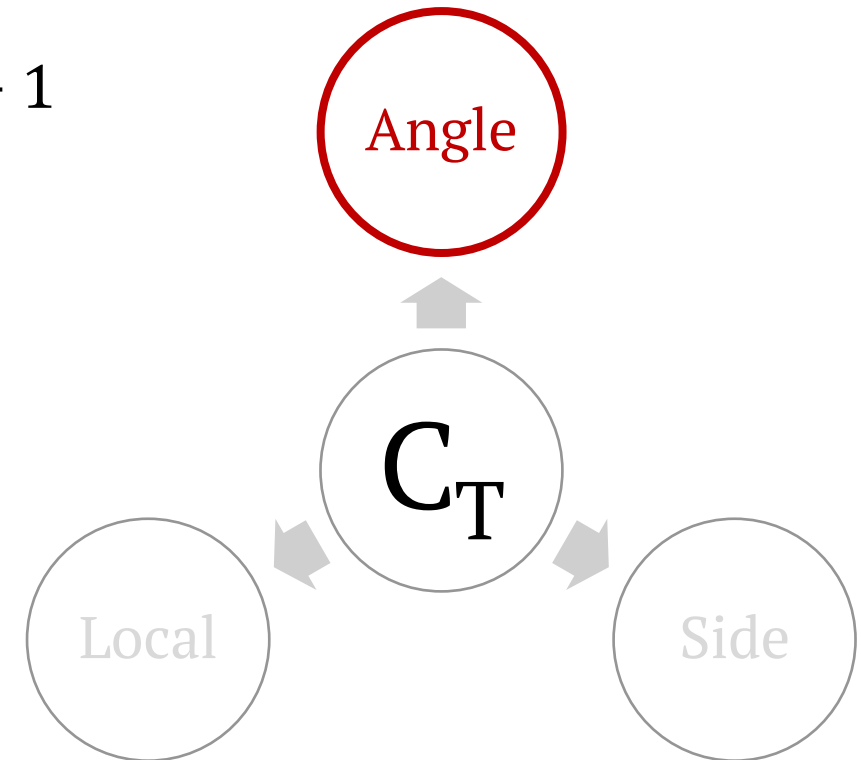
Where:

L Total number of lines.

L' Number of lines observed in one direction.

S Total number of stations.

S' Number of unoccupied stations.



(1) By Law

(2) Side Conditions

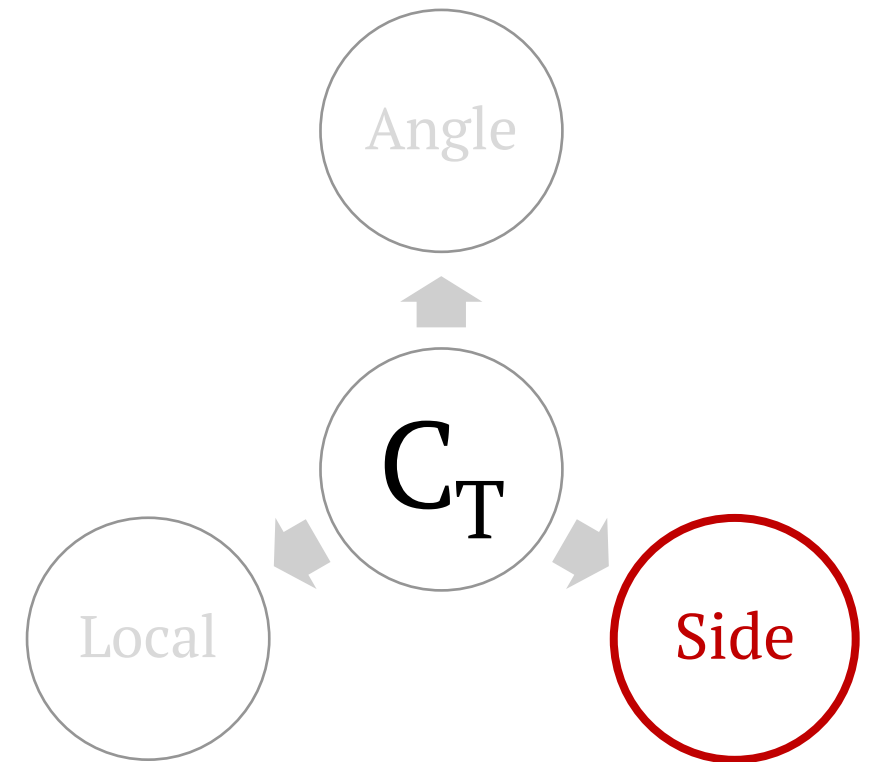
➤ The total number of side conditions C_S in a figure is:

$$C_S = L - 2S + 3$$

Where:

L Total number of lines.

S Total number of stations.



(1) By Law

(3) Local Conditions

➤ The total number of Local conditions C_{Local} in a figure is:

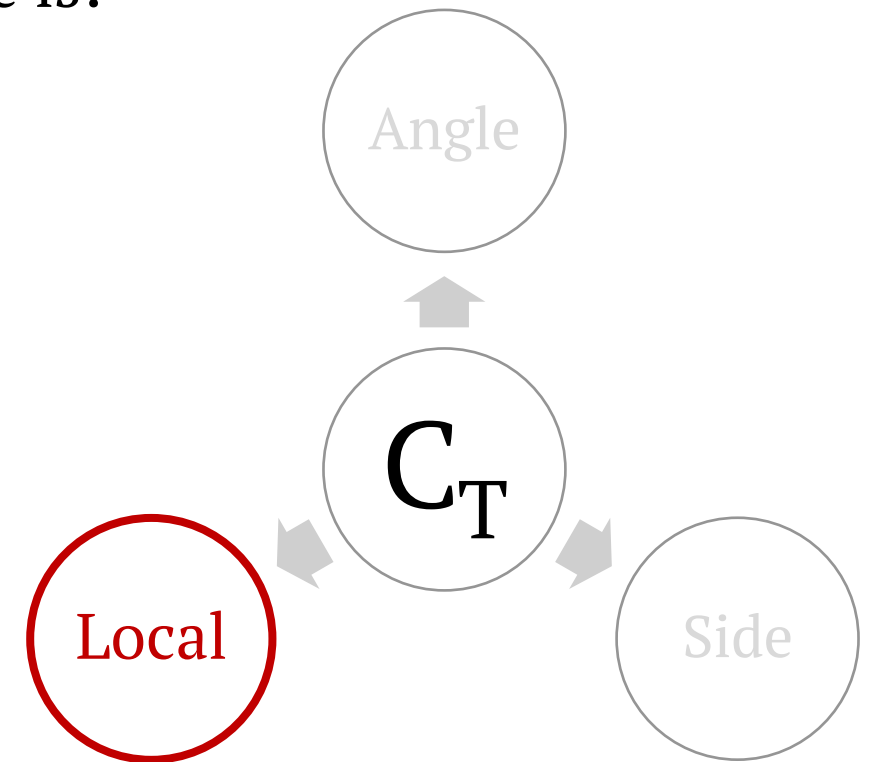
$$C_{Local} = C_T - C_A - C_S$$

Where:

C_T Total number of conditions.

C_A Total number of angle conditions.

C_S Total number of side conditions.



(1) By Law – Example

Calculate the number of different types of internal conditions in the following braced quadrilateral.

Known points = 2 (baseline)

New points = 2 (C, D)

Total number of observation $O_T = 8$

Number of necessary observations $O_{nec} = 2 \times \text{new points} = 2 \times 2 = 4$

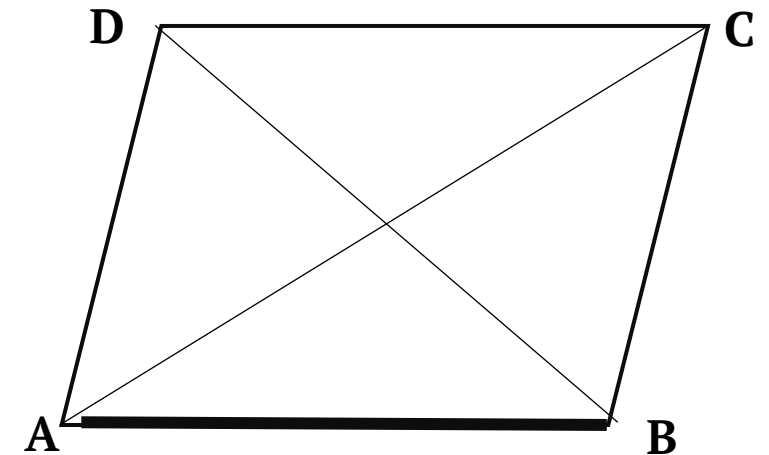
Total number of conditions $C_T = O_T - O_{nec} = 8 - 4 = 4$

Number of triangle conditions $C_A = (L - L') - (S - S') + 1$

$$= (6 - 0) - (4 - 0) + 1 = 3$$

Number of side conditions $C_S = L - 2S + 3 = 6 - 8 + 3 = 1$

Number of local conditions $C_{Local} = C_T - C_A - C_S = 4 - 3 - 1 = 0$

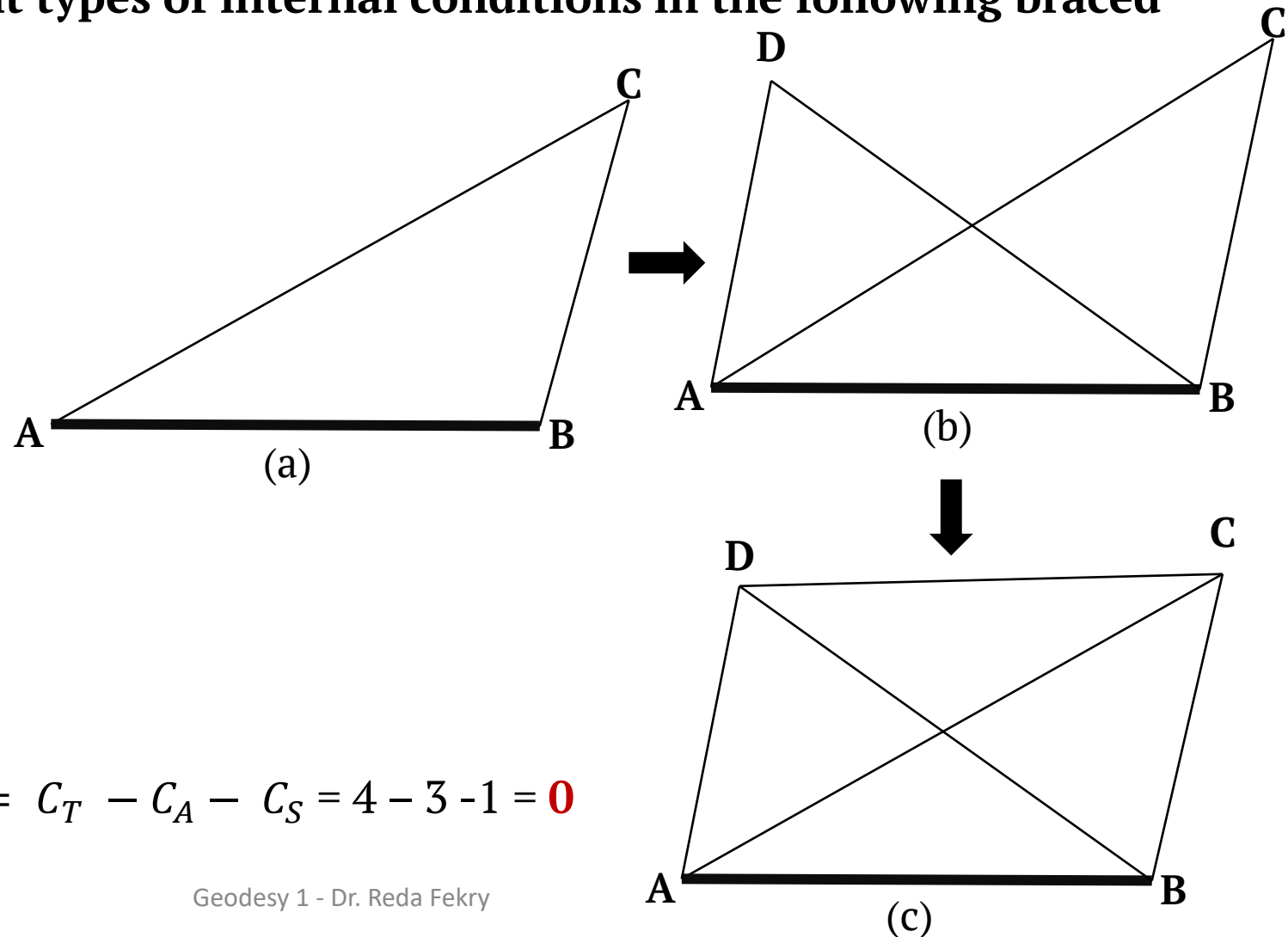


(2) Point By Point

(2) Point By Point

Calculate the number of different types of internal conditions in the following braced quadrilateral.

Point	C_A	C_S
A	-	-
B	-	-
C	$2 - 1 = 1$	$2 - 2 = 0$
D	$3 - 1 = 2$	$3 - 2 = 1$
Total	3	1



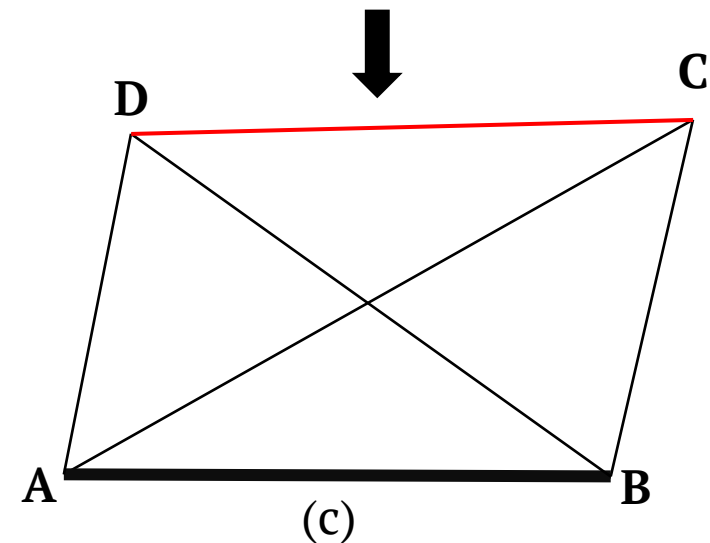
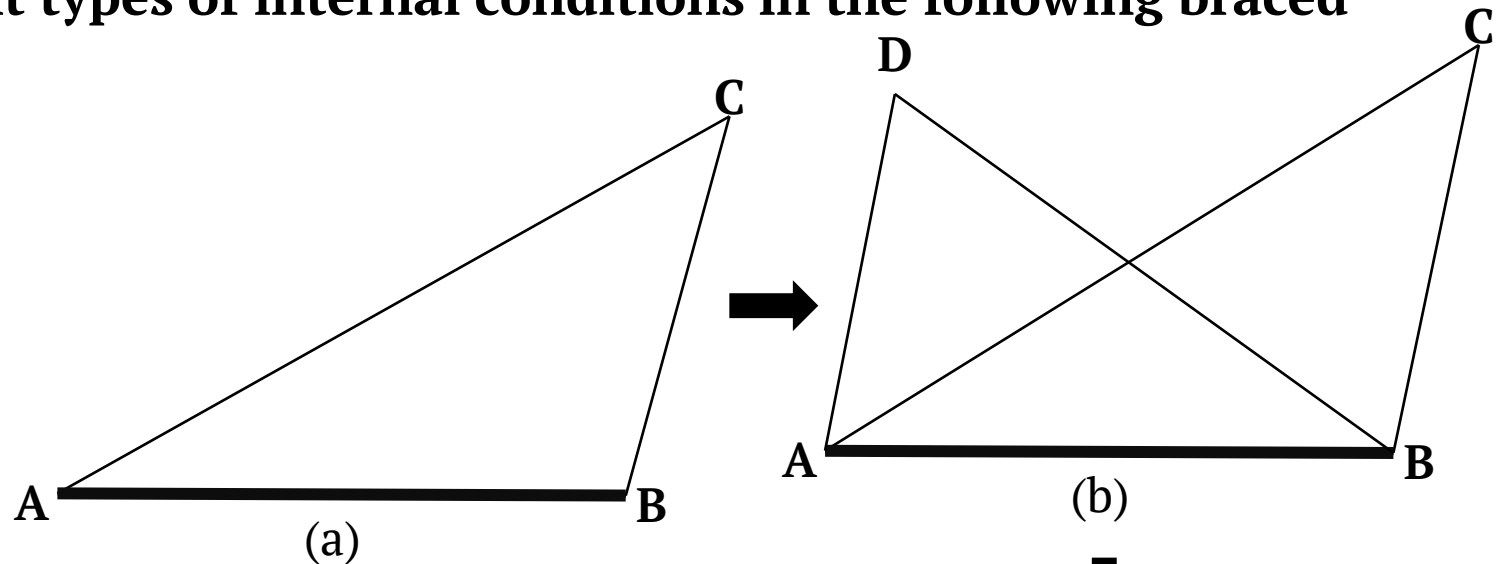
Number of local conditions $C_{Local} = C_T - C_A - C_S = 4 - 3 - 1 = 0$

(3) Triangle By Triangle

(3) Triangle By Triangle

Calculate the number of different types of internal conditions in the following braced quadrilateral.

Triangle	C_A	C_S
ABC	1	0
ABD	1	0
CD	1	1
Total	3	1



Number of local conditions $C_{Local} = C_T - C_A - C_S = 4 - 3 - 1 = 0$

Which method should be used?



Numerical Examples

(1) Calculate the number of different types of geometric conditions in the following figure:

Known points = 2 (baseline)

New points = 3 (C, D, E)

Total number of observation $O_T = 12$

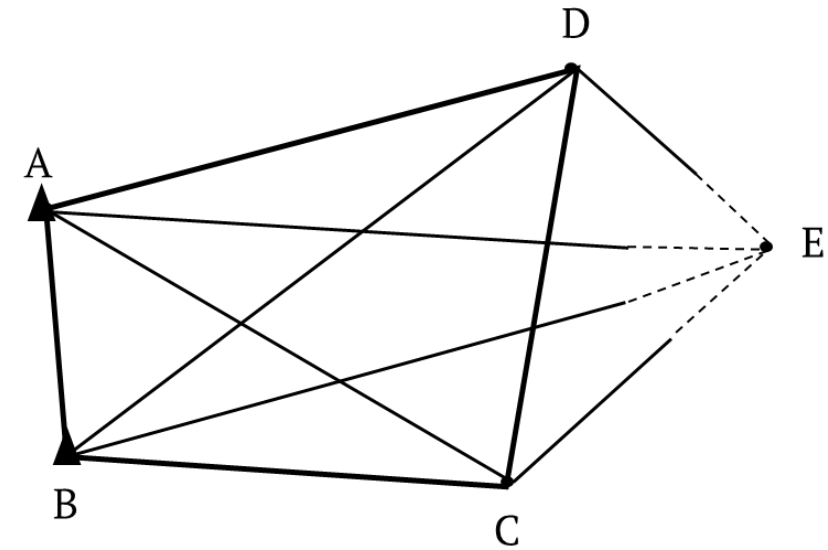
Number of necessary observations $O_{nec} = 2 \times \text{new points} = 2 \times 3 = 6$

Total number of conditions $C_T = O_T - O_{nec} = 12 - 6 = 6$

Number of triangle conditions $C_A = (L - L') - (S - S') + 1 = (10 - 4) - (5 - 1) + 1 = 3$

Number of side conditions $C_S = L - 2S + 3 = 10 - 10 + 3 = 3$

Number of local conditions $C_{Local} = C_T - C_A - C_S = 6 - 3 - 3 = 0$

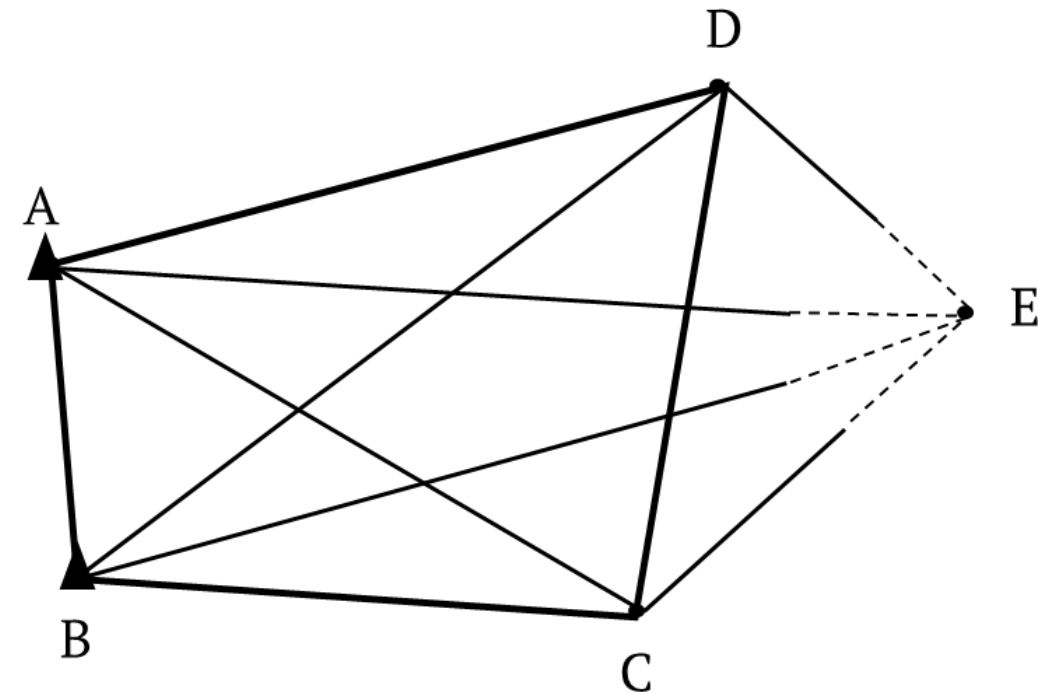


Numerical Examples

(1) Calculate the number of different types of geometric conditions in the following figure:

Point by point

Point	C_A	C_S
A	-	-
B	-	-
C	$2 - 1 = 1$	$2 - 2 = 0$
D	$3 - 1 = 2$	$3 - 2 = 1$
E	0	$4 - 2 = 2$
Total	3	3

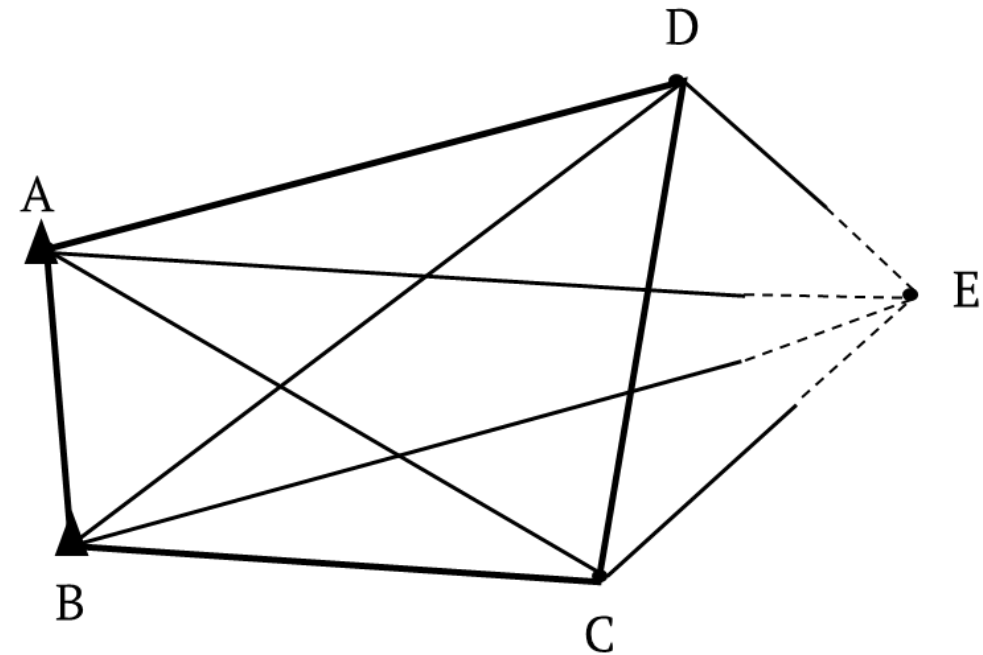


Number of local conditions $C_{Local} = C_T - C_A - C_S = 6 - 3 - 3 = 0$

(1) Calculate the number of different types of geometric conditions in the following figure:

Triangle by triangle

Triangle	C_A	C_S
ABC	1	0
ACD	1	0
CDE	0	0
BD	1	1
EA	0	1
EB	0	1
Total	3	3



$$\text{Number of local conditions } C_{Local} = C_T - C_A - C_S = 6 - 3 - 3 = \mathbf{0}$$

Numerical Examples

(2) Calculate the number of different types of geometric conditions in the following figure:

Known points = 2 (baseline)

New points = 3 (C, D, E)

Total number of observation $O_T = 13$

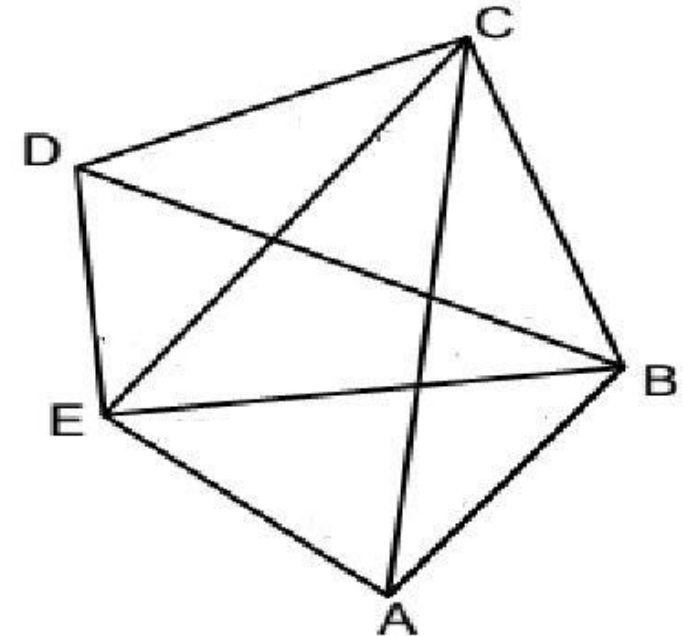
Number of necessary observations $O_{nec} = 2 \times \text{new points} = 2 \times 3 = 6$

Total number of conditions $C_T = O_T - O_{nec} = 13 - 6 = 7$

Number of triangle conditions $C_A = (L - L') - (S - S') + 1 = (9-0) - (5-0) + 1 = 5$

Number of side conditions $C_S = L - 2S + 3 = 9 - 10 + 3 = 2$

Number of local conditions $C_{Local} = C_T - C_A - C_S = 7 - 5 - 2 = 0$

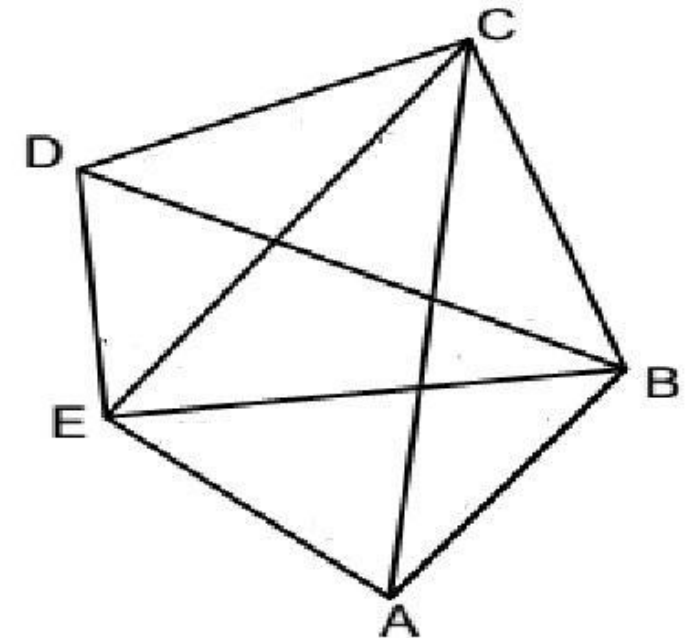


Numerical Examples

(2) Calculate the number of different types of geometric conditions in the following figure:

Point by point

Point	C_A	C_S
A	-	-
B	-	-
C	$2 - 1 = 1$	$2 - 2 = 0$
D	$2 - 1 = 1$	$2 - 2 = 0$
E	$4 - 1 = 3$	$4 - 2 = 2$
Total	5	2

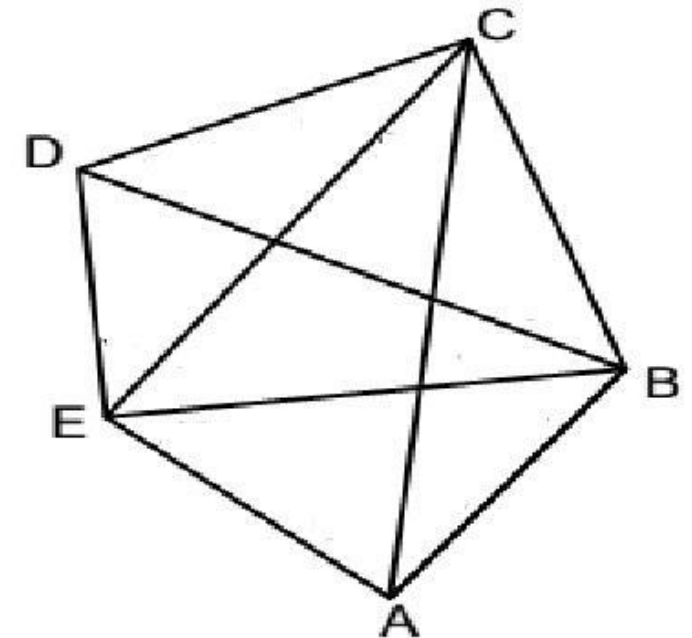


$$\text{Number of local conditions } C_{Local} = C_T - C_A - C_S = 7 - 5 - 2 = \mathbf{0}$$

(2) Calculate the number of different types of geometric conditions in the following figure:

Triangle by triangle

Triangle	C_A	C_S
ABC	1	0
ABE	1	0
EBD	1	0
EC	1	1
ED	1	1
Total	5	2



$$\text{Number of local conditions } C_{Local} = C_T - C_A - C_S = 7 - 5 - 2 = 0$$

Numerical Examples

(3) Calculate the number of different types of geometric conditions in the following figure:

Known points = 2 (baseline)

New points = 3 (C, D, M)

Total number of observation $O_T = 12$

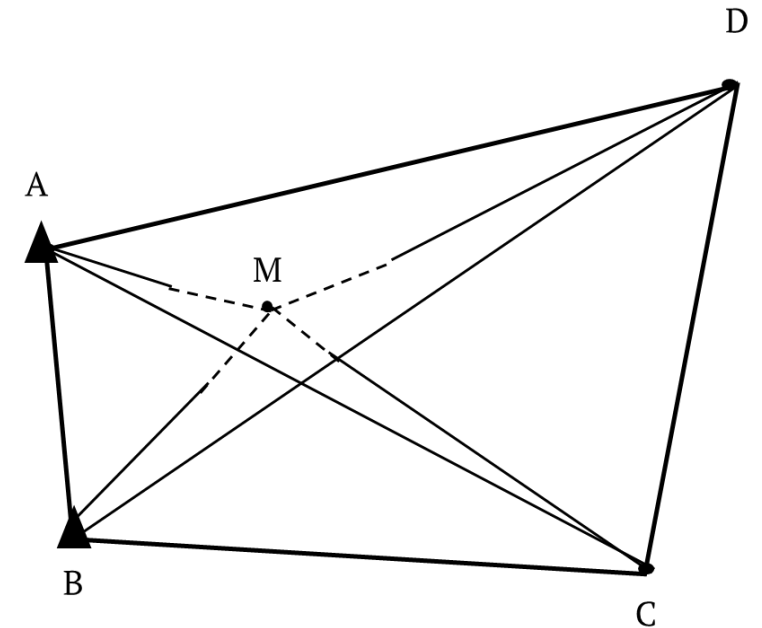
Number of necessary observations $O_{nec} = 2 \times \text{new points} = 2 \times 3 = 6$

Total number of conditions $C_T = O_T - O_{nec} = 12 - 6 = 6$

Number of triangle conditions $C_A = (L - L') - (S - S') + 1 = (10 - 4) - (5 - 1) + 1 = 3$

Number of side conditions $C_S = L - 2S + 3 = 10 - 10 + 3 = 3$

Number of local conditions $C_{Local} = C_T - C_A - C_S = 6 - 3 - 3 = 0$

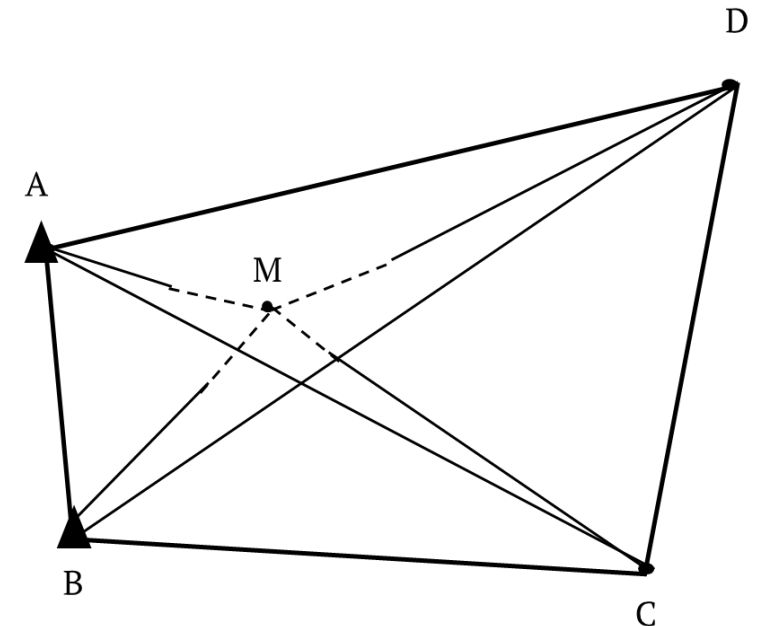


Numerical Examples

(3) Calculate the number of different types of geometric conditions in the following figure:

Point by point

Point	C_A	C_S
A	-	-
B	-	-
C	$2 - 1 = 1$	$2 - 2 = 0$
D	$3 - 1 = 2$	$3 - 2 = 1$
M	0	$4 - 2 = 2$
Total	3	3



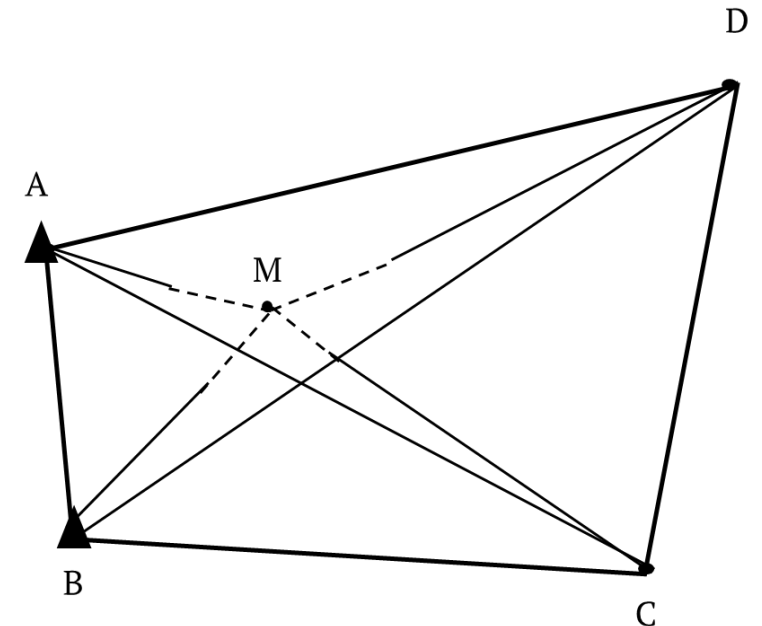
$$\text{Number of local conditions } C_{Local} = C_T - C_A - C_S = 6 - 3 - 3 = \mathbf{0}$$

Numerical Examples

(3) Calculate the number of different types of geometric conditions in the following figure:

Triangle by triangle

Triangle	C_A	C_S
ABC	1	0
ABD	1	0
ABM	0	0
CD	1	1
MD	0	1
MC	0	1
Total	3	3



$$\text{Number of local conditions } C_{Local} = C_T - C_A - C_S = 6 - 3 - 3 = 0$$

Numerical Examples

(4) Calculate the number of different types of geometric conditions in the following figure:

Known points = 2 (baseline)

New points = 1 (M)

Total number of observation $O_T = 12$

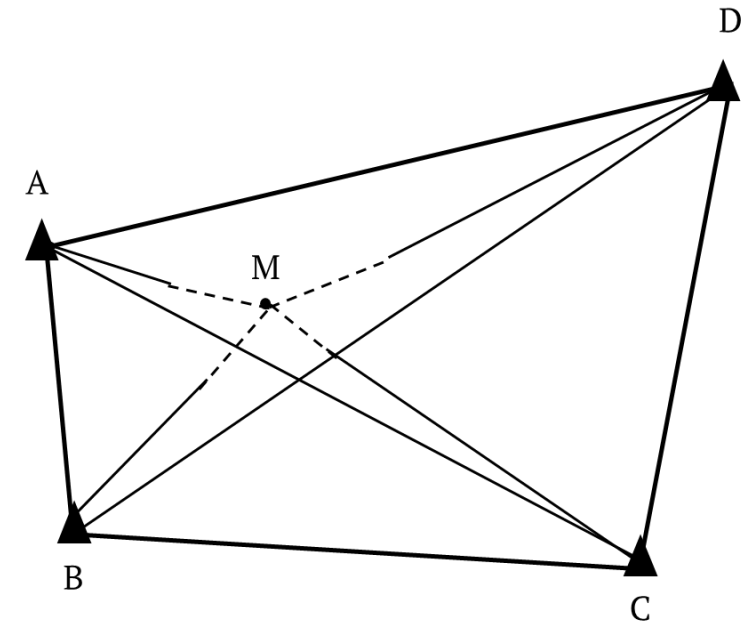
Number of necessary observations $O_{nec} = 2 \times \text{new points} = 2 \times 1 = 2$

Total number of conditions $C_T = O_T - O_{nec} = 12 - 2 = 10$

Number of triangle conditions $C_A = (L - L') - (S - S') + 1 = (10 - 4) - (5 - 1) + 1 = 3$

Number of side conditions $C_S = L - 2S + 3 = 10 - 10 + 3 = 3$

Number of local conditions $C_{Local} = C_T - C_A - C_S = 10 - 3 - 3 = 4$

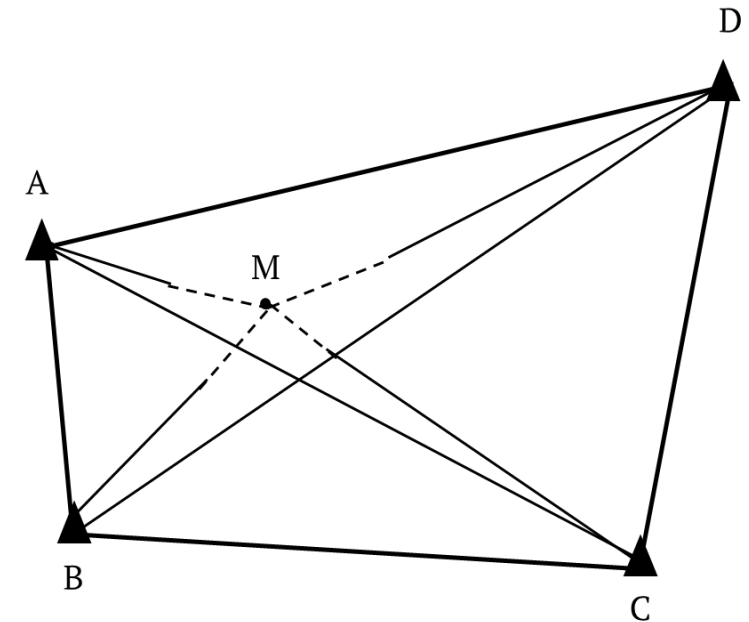


Numerical Examples

(4) Calculate the number of different types of geometric conditions in the following figure:

Point by point

Point	C_A	C_S
A	-	-
B	-	-
C	$2-1 = 1$	$2-2 = 0$
D	$3-1 = 2$	$3-2 = 1$
M	-	$4-2 = 2$
Total	3	3

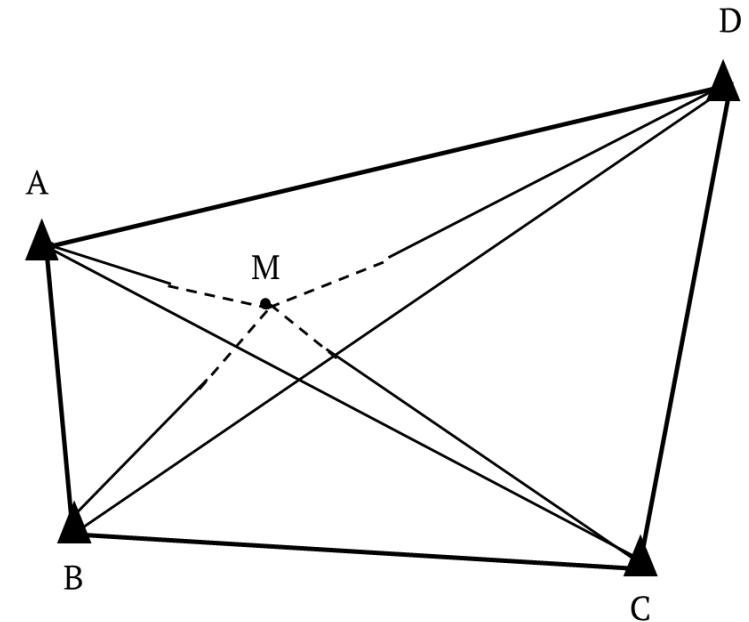


$$\text{Number of local conditions } C_{Local} = C_T - C_A - C_S = 10 - 3 - 3 = 4$$

(4) Calculate the number of different types of geometric conditions in the following figure:

Triangle by triangle

Triangle	C_A	C_S
ABC	1	0
ABD	1	0
ABM	0	0
CD	1	1
MD	0	1
MC	0	1
Total	3	3



$$\text{Number of local conditions } C_{Local} = C_T - C_A - C_S = 10 - 3 - 3 = 4$$

End of Presentation

THANK YOU

